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[TP] At 25°C  
 $E = E^\circ - (0.06/n_e) V \log(Q)$   
 What is the value of  $E$  when everything is in **standard states**?

0% 1.  $E = \infty$   
 0% 2.  $E = 0$   
 50% 3.  $E = E^\circ$   
 0% 4. None of the above  
 50% 5. Not sure

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Lecture 18 CH131 Summer 1 2021  
 Wednesday, June 30, 2021

- Complete: What determines cell voltage,  $E_{\text{cell}}$ ?
- Practice problems
- Questions?

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$E = -(0.06/n_e) V \log(Q/K)$

The value of  $E$  when  $Q = 1$  at 25 °C is  
 $E(Q = 1) = E^\circ + (0.06/n_e) V \log(K)$  ✓

Calculate  $K$  corresponding to  $E^\circ = 1.8 V$  for  $n_e = 1$ .  
 $K = 10^{30}$ . Very large!

$\frac{1.8}{0.06} = 30$   
 $K = 10^{+30}$  //  
 $A + B \rightleftharpoons C + D$   
 $Q = \frac{1 \cdot 1 \cdot 1 \cdot 1}{1 \cdot 1} = 1$   
 $E = E^\circ = 1.8 V$   
 $Q = K = 10^{+30}$   
 $\text{no no } \rightleftharpoons \text{no no}$

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 What is the value of  $E$  when everything is in **standard states**?

0% 1.  $E = \infty$   
 0% 2.  $E = 0$   
 100% 3.  $E = E^\circ$  //  
 0% 4. None of the above  
 0% 5. Not sure

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[TP] At 25°C  
 $E = E^\circ - (0.06/n_e) V \log(Q)$   
 What is the value of  $E$  when everything is at equilibrium?

0% 1.  $E = \infty$   
 100% 2.  $E = 0$  //  
 0% 3.  $E = E^\circ$   
 0% 4. None of the above  
 0% 5. Not sure

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### Electrochemistry practice problems

- ✓ 17.15 Reduction potential from cell potential
- ✓ 17.33 Concentration from cell potential
- ~~✗ 17.35 Equilibrium constant from cell potential~~
- ✓ 17.41  $K_{sp}$  from cell potential

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### Electrochemistry practice problem: 17.15

15. In a galvanic cell, one half-cell consists of a zinc strip dipped into a 1.00 M solution of  $Zn(NO_3)_2$ . In the second half-cell, solid indium adsorbed on graphite is in contact with a 1.00 M solution of  $In(NO_3)_3$ . Indium is observed to plate out as the galvanic cell operates, and the initial cell potential is measured to be 0.425 V at 25°C.

(a) Write balanced equations for the half-reactions at the anode and the cathode.  
 (b) Calculate the standard reduction potential of an  $In^{3+} | In$  half-cell. Consult Appendix E for the reduction potential of the  $Zn^{2+} | Zn$  electrode.

Handwritten work:  
 $E_{cell} = 0.425 V = E^\circ_{cathode} - E^\circ_{anode}$   
 $0.425 = E^\circ_{In} - (-0.7628)$   
 $E^\circ_{In} = 0.425 - 0.7628 = -0.338 V$   
 $Q = \frac{[Zn^{2+}]}{[In^{3+}]^3} = \frac{1}{1^3} = 1$

2  $(In^{3+} + 3e^- \rightarrow In(s))$  cathode  
 3  $(Zn(s) \rightarrow Zn^{2+}(aq) + 2e^-)$  anode  
 $2 In^{3+} + 3 Zn(s) \rightarrow 2 In(s) + 3 Zn^{2+}(aq)$   
 $K =$

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### Electrochemistry practice problem: 17.33

33. The following reaction occurs in an electrochemical cell:  
 $3 HClO_2(aq) + 2 Cr^{3+}(aq) \rightleftharpoons 12 H_2O(l) + 3 HClO(aq) + Cr_2O_7^{2-}(aq) + 8 H_3O^+(aq)$

(a) Calculate  $E^\circ$  for this cell.  
 (b) At pH 0, with  $[Cr_2O_7^{2-}] = 0.80 M$ ,  $[HClO_2] = 0.15 M$ , and  $[HClO] = 0.20 M$ , the cell potential is found to be 0.15 V. Calculate the concentration of  $Cr^{3+}(aq)$  in the cell.

Handwritten work:  
 (a)  $E^\circ = 0.31 V$   
 (b)  $[Cr^{3+}] = 1.09 \times 10^{-8} M$   
 $0.15 = -\frac{0.0592}{6} \log(Q) + 0.31$   
 $-0.16 = -\frac{0.0592}{6} \log(Q)$   
 $\frac{6 \times 0.16}{0.0592} = \log(Q)$   
 $Q = 10$   
 $Q = \frac{[Cr_2O_7^{2-}][H_3O^+]^8 [HClO]^3}{[HClO_2]^3 [Cr^{3+}]^2}$   
 $10 = \frac{(0.80)(1)^8 (0.20)^3}{(0.15)^3 x^2}$

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### Electrochemistry practice problem: 17.35

$K = 3 \times 10^{31}$ , so orange

35. By using the half-cell potentials in Appendix E, calculate the equilibrium constant at 25°C for the reaction in problem 33. Dichromate ion (orange) and  $\text{Cr}^{3+}$  is light green in aqueous solution. If 2.00 L of 1.00 M  $\text{HClO}_2$  solution is added to 2.00 L of 0.30 M  $\text{Cr}(\text{NO}_3)_3$  solution, what color will the resulting solution have?

$$3 \text{HClO}_2 + \text{Cr}_2\text{O}_7^{2-} + 12 \text{H}_2\text{O} \rightarrow 3 \text{HClO} + \text{Cr}_2\text{O}_7^{2-} + 8 \text{H}_3\text{O}^+$$

|    |         |        |       |       |      |
|----|---------|--------|-------|-------|------|
| I  | 0.500   | 0.750  | 0     | 0     | 0    |
| CI | -0.375  | -0.250 | 0     | 0     | 0    |
| C  | 0.125   | 0      | 0.375 | 0.125 | 1.00 |
| E  | +3y     | +2y    | -3y   | -y    | -8y  |
|    | ≈ 0.125 | 2y     | 0.375 | 0.125 | 1.00 |

$3 \times 10^{31} = \frac{(0.375)^3 (0.125)(1.00)}{(0.125)(2y)^2}$  y really small

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### Electrochemistry practice problem: 17.41

$E^\circ = 1.065 \text{ V}$   
 $K_{sp} = 7.5 \times 10^{-13}$

41. A galvanic cell is constructed in which the overall reaction is  
 $\text{Br}_2(\ell) + \text{H}_2\text{O}(\text{g}) + 2 \text{H}_2\text{O}(\ell) \rightarrow 2 \text{Br}^-(\text{aq}) + 2 \text{H}_3\text{O}^+(\text{aq})$

(a) Calculate  $E^\circ$  for this cell.  
 (b) Silver ions are added until  $\text{AgBr}$  precipitates at the cathode and  $[\text{Ag}^+]$  reaches 0.060 M. The cell potential is then measured to be 1.710 V at pH = 0 and = 1.0 atm. Calculate  $[\text{Br}^-]$  under these conditions.  
 (c) Calculate the solubility product constant  $K_{sp}$  for  $\text{AgBr}$ .

$1.710 = 1.065 - \frac{0.0592}{2} \log([\text{Br}^-])^2$   
 $[\text{Br}^-] = 1.3 \times 10^{-11}$

$\text{AgBr}(s) \rightleftharpoons \text{Ag}^+(\text{aq}) + \text{Br}^-(\text{aq})$   
 $E = \text{ppt} - \frac{0.060}{1.3 \times 10^{-11}}$   
 $K_{sp} = [\text{Ag}^+][\text{Br}^-] = (0.060)(1.3 \times 10^{-11}) = 7.6 \times 10^{-13}$

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Quiz 5, 8.5.

$$\text{Pb}(\text{IO}_3)_2(s) \rightleftharpoons \text{Pb}^{2+}(\text{aq}) + 2 \text{IO}_3^-(\text{aq})$$

I

$[\text{Pb}^{2+}] = 0.0600 \text{ L} \times 0.0500 \text{ mol/L} = 0.00300 \text{ mol} / 0.105 \text{ L} = 0.0286$   
 $[\text{IO}_3^-] = 0.0490 \text{ L} \times 0.300 \text{ mol/L} = 0.0135 \text{ mol} / 0.105 \text{ L} = 0.129$

$Q_{sp} = [\text{Pb}^{2+}][\text{IO}_3^-]^2 = 0.000472$

$K_{sp} = [\text{Pb}^{2+}][\text{IO}_3^-]^2 = 2.6 \times 10^{-13}$

$X = K_{sp} / (0.0714)^2$

|                  |          |            |  |
|------------------|----------|------------|--|
|                  | 0.00300  | 0.0135     |  |
| $\text{Pb}^{2+}$ | 0.00300  | 0.0135     |  |
| $\text{IO}_3^-$  | -0.00600 | -0.0270    |  |
|                  | 0        | 0.0714     |  |
|                  | -X       | +X         |  |
|                  | 0.00300  | 0.0714 + X |  |

$5.1 \times 10^{-11} = -X$

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### Oxley / problem 51

$0.1000 \text{ L} \times 0.3750 \text{ mol/L} \text{ Ba}(\text{OH})_2(s) \rightleftharpoons \text{Ba}^{2+}(\text{aq}) + 2 \text{OH}^-(\text{aq})$   
 $= 0.03750 \text{ mol OH}^-$   
 $= 0.07500 \text{ mol OH}^-$

$0.4540 \text{ M HClO}_2$   
 $\text{Ba}(\text{OH})_2(\text{aq}) + 2 \text{HClO}_2(\text{aq}) \rightarrow \text{Ba}(\text{ClO}_2)_2(\text{aq}) + 2 \text{H}_2\text{O}(\ell)$

① No acid added:  $[\text{OH}^-] = 0.07500 \text{ mol OH}^- / 0.1000 \text{ L} = 0.7500 \text{ mol OH}^- / \text{L}$

②  $0.07500 \text{ mol OH}^- = V_a \times 0.4540 \text{ mol/L}$   
 $V_a = \frac{0.07500 \text{ mol}}{0.4540 \text{ mol/L}} = 0.165 \text{ L}$

$[\text{OH}^-] = \frac{0.07500 \text{ mol} - 0.164 \text{ L} \times 0.4540 \text{ mol/L}}{0.1000 \text{ L} + 0.164 \text{ L}}$

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$$\text{HA} + \text{H}_2\text{O} \rightleftharpoons \text{H}_3\text{O}^+ + \text{A}^- \quad K_a$$

① pure weak acid }  $\text{HA} + \text{H}_2\text{O} \rightleftharpoons \text{H}_3\text{O}^+ + \text{A}^-$   
 ② some acid neutralized }  
 ③ equivalence }  $\text{A}^- + \text{H}_2\text{O} \rightleftharpoons \text{HA} + \text{OH}^- \quad K_b = \frac{K_w}{K_a}$   
 ④ excess OH }  $\left[ \frac{\text{left over mol of OH}^-}{\text{total volume}} \right] \rightarrow [\text{H}_3\text{O}^+]$

$$R = 8.314 \frac{\text{J}}{\text{mol K}}$$

$$P_2 = \frac{J}{\text{m}^3}$$

$$J = P_2 \text{ m}^3$$

$$= \frac{1}{101325} \text{ atm} * 1000 \text{ L}$$

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